

DIRECTIONS: Please clearly print your name on each page. You are allowed to use your calculator and the attached formula sheet. This exam consists of two parts.

Part A has four multiple choice questions each worth 4 points, answer *all* of these.

Part B has four problems (each worth 28 points). You are required to solve three out of these four problems.

You **MUST** indicate on the chart below which **three** problems you choose to be graded.

Question 1	/4
Question 2	/4
Question 3	/4
Question 4	/4
Problem __	/28
Problem __	/28
Problem __	/28
Total	/100

Part A: Multiple choice questions
(4 points each)

Please answer each question by circling the letter of the best answer.

Question 1: An object placed at the center of curvature of a concave mirror ($R > 0$) produces:

- a) No image.
- b) An image at infinity.
- c) A virtual image a distance R behind the mirror.
- d) A real image at the center of curvature, R .
- e) A virtual image at the focus, $R/2$.
- f) A real image a distance $R/2$ behind the mirror.

Question 2: The velocity of propagation for the pair of electromagnetic fields given by $\vec{E} = E_m \cos(kz - t\omega)\hat{j}$ and $\vec{B} = B_m \cos(kz - t\omega)\hat{i}$ is

- a) $\vec{v} = c\hat{i}$
- b) $\vec{v} = c\hat{j}$
- c) $\vec{v} = c\hat{k}$
- d) $\vec{v} = -c\hat{i}$
- e) $\vec{v} = -c\hat{j}$
- f) $\vec{v} = -c\hat{k}$

Question 3: A helium-neon laser (wavelength = 632.8 nm) is incident on a container of liquid with index of refraction $n_{\text{liquid}} = 1.23$. Consider the index of refraction of air as $n_{\text{air}} = 1$. Which of the following statements is true?

- a) The frequency in the liquid is less than the frequency in air.
- b) The wavelength in the liquid is larger than the wavelength in air.
- c) The laser light travels faster in the liquid.
- d) Total internal reflection occurs for every possible angle of incidence from air into the liquid.
- e) None of these.

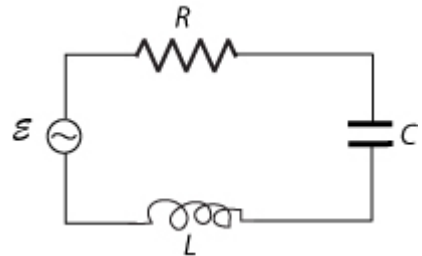
Question 4: Unpolarized light of intensity I_0 is passed through two polarizers whose transmission axes make a 60° angle with respect to each other. (*Hint: Remember to consider the intensity after passing through the first polarizer.*) After the light passes through both polarizers, it has an intensity given by:

- a) $3 I_0/8$
- b) $I_0/8$
- c) $7 I_0/16$
- d) $I_0/2$
- e) $I_0/6$

Part B: Problems (28 points each)

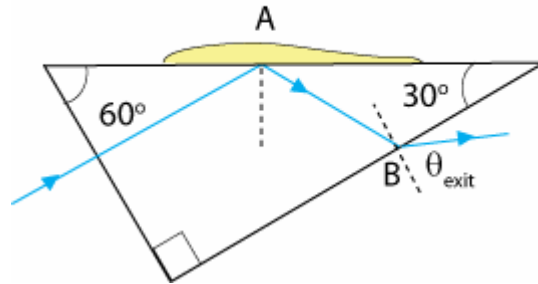
Please show all of your calculations and reasoning. Missing or incorrect work will earn no credit.

Problem 1: A single loop RCL series circuit is driven by an alternating emf given by $\mathcal{E} = \mathcal{E}_0 \sin \omega t$ where $\mathcal{E}_0 = 10\text{V}$. You are given that the frequency is $f = 60\text{ Hz}$, the inductance is $L=0.11\text{ H}$ and the resistance. The current leads the emf, \mathcal{E} , by 37° .



- What is the capacitance in the circuit?
- What is the impedance of the circuit?
- At resonance what is the value of the current amplitude (I_0)?
- What is the average power dissipated in (i) the resistor, (ii) the capacitor and (iii) the inductor?

Problem 2: Light is incident normally on the short face of a 30° - 60° - 90° prism. The index of refraction of the prism is $n = 1.62$.

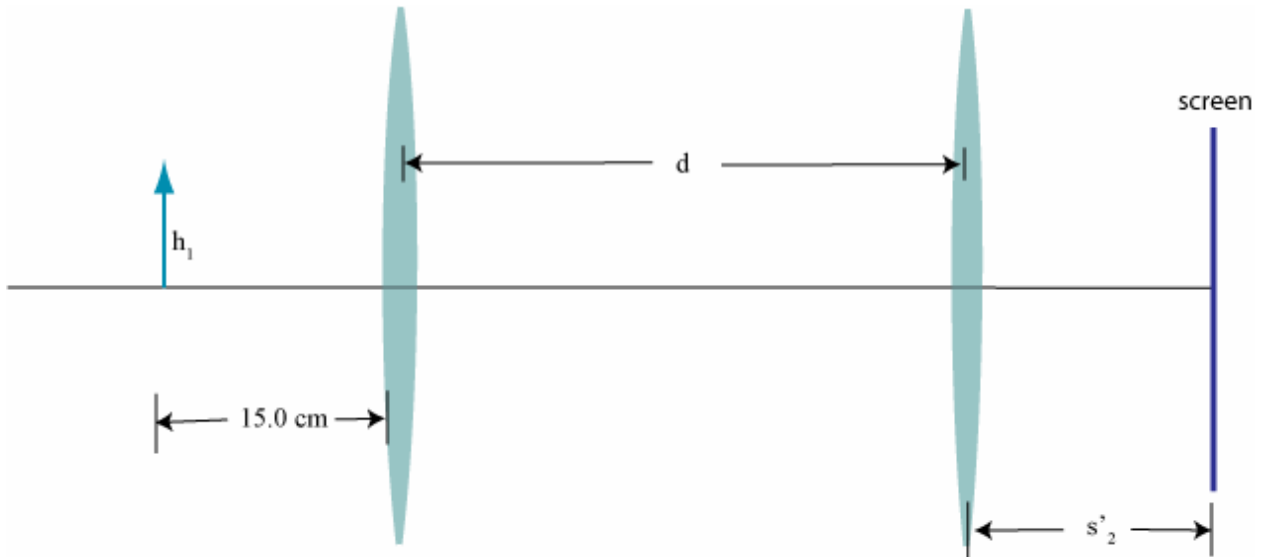


- A drop of liquid is placed on the hypotenuse of the prism. Find the maximum index of refraction for the liquid so that the light will be totally reflected.
- If such total internal reflection occurs, find the value of θ_{exit} , the exit angle at point B (into air which has an index of refraction of 1).
- If the liquid on the hypotenuse were wiped away and then replaced with a drop of liquid having an index of refraction equal to 1.82, explain why the intensity of light exiting at point B suddenly drops.

Problem 3: A small circular target with a diameter of 5.00 cm faces a monochromatic light source that is 4.33 m away. At the target the electric field amplitude of the light from the source is 1.27×10^3 V/m. (*Hint: Recall that power is measured in watts, energy is measured in joules, intensity is measured in watts per square meter, and pressure in pascals. Also $1 \text{ Pa} = 1 \text{ N/m}^2$ and $1 \text{ W} = 1 \text{ J/s}$.)*)

- a) What is the amplitude of the magnetic field at the target?
- b) What is the intensity from the light source at the target?
- c) Assuming the target is 100 % absorptive, what is the average radiation pressure exerted by the light on the mirror?
- d) What is the force felt by the target?
- e) What is the total radiant power output of the source if it is assumed to radiate uniformly in all directions?

Problem 4: You are given two thin lenses with focal lengths, $f_1 = 12.0$ cm and $f_2 = 7.50$ cm separated by a distance, $d=70.0$ cm. Placing an object 15.0 cm to the left of the first lens (f_1) will produce a real image on the screen at the right.



- Are these lenses both converging, both diverging or one of each?
- What is position of this final image, s'_2 , with respect to the second lens?
- Is the final image erect or inverted?
- If the original object has a height of $h_1 = 8.50$ mm, what is the height of the final image?